

Рождение пары мюонов на БАК в процессе, индуцированном фотонами, в модели с дополнительной размерностью и малой кривизной пространства-времени

А.В. Киселев

Отдел теоретической физики
НИЦ «Курчатовский институт» - ИФВЭ

(совместно с: *Salih Inan, Cumhuriyet University, Turkey*)

Опубликовано в: EPJC, 78 (2018) 729

Семинар ОТФ, 9 октября 2018 года

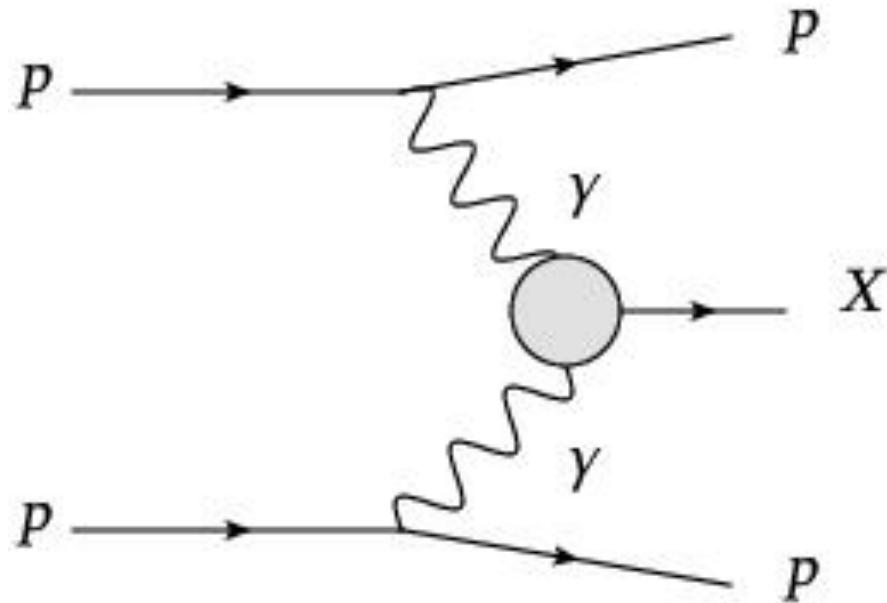
*...всего натуральнее было бы постановить,
что только те науки распространяют свет,
кои способствуют выполнению
начальственных предписаний.*

М.Е. Салтыков -Щедрин,
«Дневник провинциала в Петербурге»

План доклада

- Эксклюзивное рождение в столкновении фотонов и его экспериментальное изучение.
- Модель Рандалл-Сундрума (РС) с одной дополнительной размерностью и ее обобщение.
- Процесс на БАК, индуцированный фотонами. Приближение эквивалентных фотонов.
- Дифференциальное и полное сечения для процесса $p\bar{p} \rightarrow p\gamma\gamma p \rightarrow p\mu^+\mu^-p$ при энергии 14 ТэВ в РС модели с малой кривизной пространства-времени.
- Заключение.

Photon-induced exclusive production



Schematic diagram for the reaction $pp \rightarrow p\gamma\gamma p \rightarrow pXp$
($X = \mu^+\mu^-, e^+e^-, \gamma\gamma, WW, ZZ, H, \text{etc.}$)

Forward detectors at the LHC can detect intact outgoing protons in interval:

$$\xi_{\min} < \xi < \xi_{\max}$$

where ξ is momentum fraction loss of the proton

Acceptance ranges:

ATLAS Forward Physics Collaboration (AFP)

$$0.0015 < \xi < 0.15$$
$$0.015 < \xi < 0.15$$

CMS-TOTEM Precision Proton Spectrometer (CT-PPS)

$$0.0015 < \xi < 0.5$$
$$0.1 < \xi < 0.5$$

Experimental studies of photon-induced reactions

Tevatron, CDF Collaboration, 2009:

$$pp \rightarrow p\gamma\gamma p \rightarrow pl^+l^-p \quad (l = e, \mu)$$

LHC (7 TeV), CMS Collaboration, 2012:

$$pp \rightarrow p\gamma\gamma p \rightarrow pl^+l^-p \quad (l = e, \mu)$$

LHC (7 TeV), ATLAS Collaboration, 2014:

$$pp \rightarrow p\gamma\gamma p \rightarrow pl^+l^-p \quad (l = e, \mu)$$

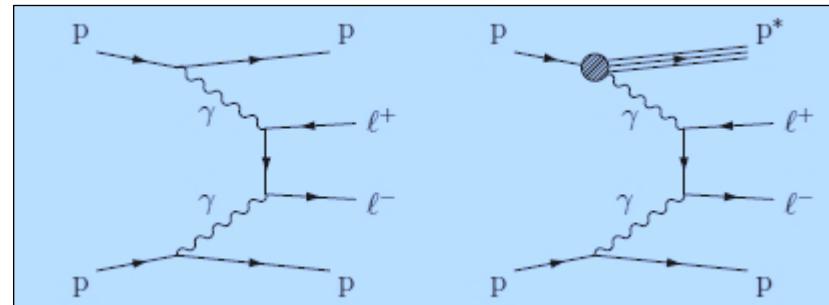
LHC (8 TeV), ATLAS Collaboration, 2016:

$$pp \rightarrow p\gamma\gamma p \rightarrow pl^+l^-p \quad (l = e, \mu)$$

First observation
of **proton-tagging**
 $\gamma\gamma$ collision:

**LHC (13 TeV), CMS-TOTEM
Collaboration, 2018**

$$pp \rightarrow p\gamma\gamma p^* \rightarrow pl^+l^-p^* \\ m(l^+l^-) > 110 \text{ GeV} \\ 12 \mu^+\mu^- , 8 e^+e^-$$



Randall-Sundrum scenario

Background metric (y is extra coordinate)

$$ds^2 = e^{-2\sigma(y)} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2$$

warp factor



Periodicity: $(x, y \pm 2\pi r_c) = (x, y)$

\mathbb{Z}_2 -symmetry: $(x, y) = (x, -y)$

→ orbifold S^1/\mathbb{Z}_2 $0 \leq y \leq \pi r_c$

Two fixed points: $y=0$ and $y= \pi r_c$

→ two (1+3)-dimensional branes

5-dimensional action $S = S_g + S_1 + S_2$

$$S_g = \int d^4x \int dy \sqrt{G} \left(2M_5^3 R^{(5)} - \Lambda \right) \quad (\text{gravity term})$$

$$S_{1(2)} = \int d^4x \sqrt{g_{1(2)}} \left(L_{1(2)} - \Lambda_{1(2)} \right) \quad (\text{brane terms})$$

Einstein-Hilbert's equations:

$$\sigma'^2(y) = -\frac{\Lambda}{24M_5^3}$$

$$\sigma''(y) = \frac{1}{12M_5^3} [\Lambda_1 \delta(y) + \Lambda_2 \delta(\pi r_c - y)]$$

Original Randall-Sundrum solution

(Randall & Sundrum, 1999)

$$\sigma_{\text{RS}}(y) = \kappa |y| \quad \Lambda_{\text{RS}} = -24M_5^3\kappa^2, \quad (\Lambda_1)_{\text{RS}} = -(\Lambda_2)_{\text{RS}} = 24M_5^3\kappa$$



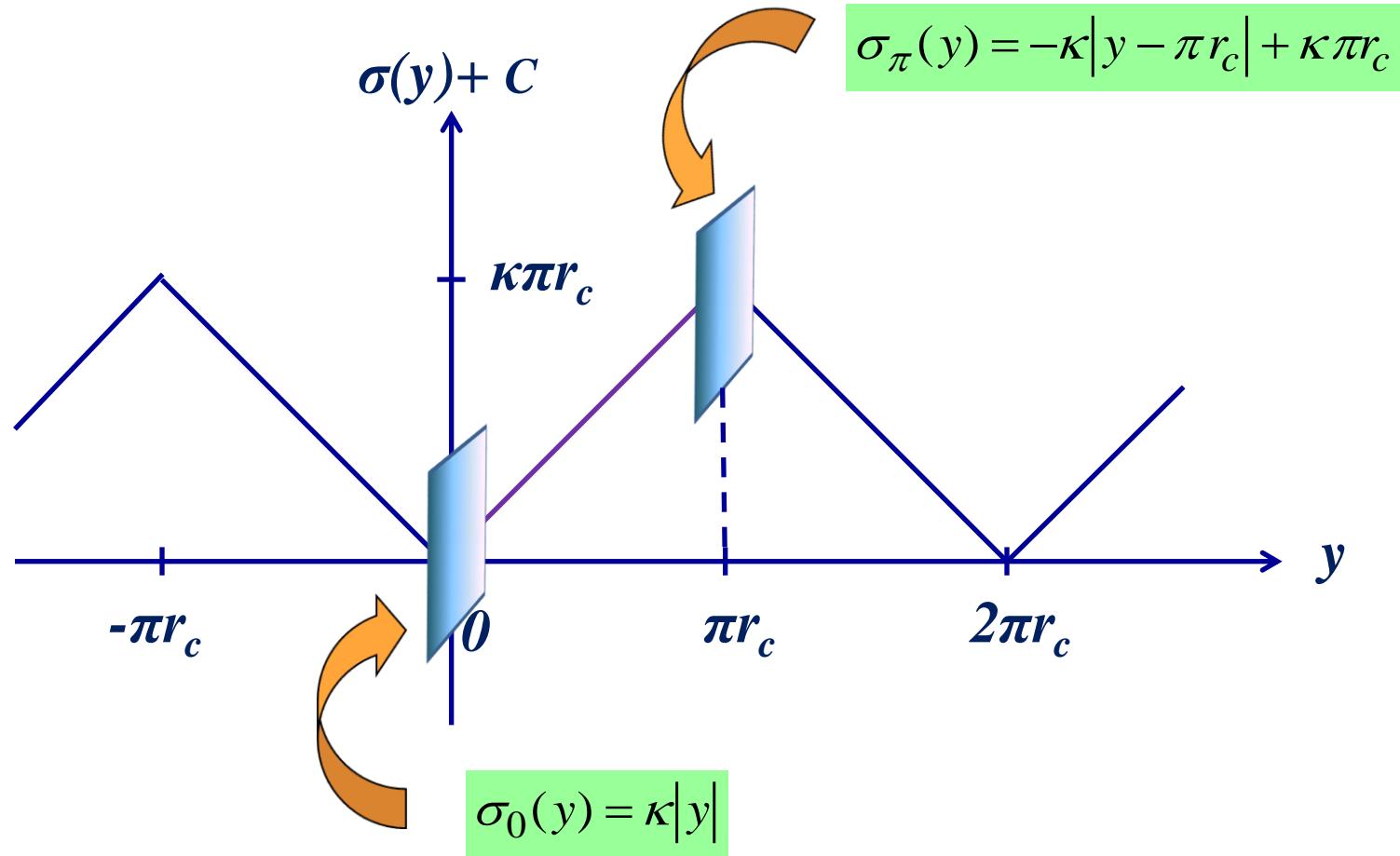
$$\sigma'_{\text{RS}}(y) = \kappa \varepsilon(y) \quad \sigma''_{\text{RS}}(y) = 2\kappa \delta(y)$$

The RS solution:

- does not explicitly reproduce the jump on TeV brane (at $y=\pi r_c$)
- is not symmetric with respect to both branes (located at $y=0$ and $y=\pi r_c$)
- does not include a constant term

Generalization of RS solution

Two equivalent solutions related to different branes



→ Generalized solution $(0 \leq C \leq \kappa\pi r_c)$

$$\sigma(y) = \frac{1}{2} [\sigma_0(y) + \sigma_\pi(y)] - C = \frac{\kappa}{2} (|y| - |y - \pi r_c|) + \frac{\kappa\pi r_c}{2} - C$$

with fine tuning

$$\Lambda = -24M_5^3\kappa^2, \quad \Lambda_1 = -\Lambda_2 = 12M_5^3\kappa$$

1-st derivative of $\sigma(y)$



*factor of 2 different
than that of RS*

$$\sigma'(y) = \frac{\kappa}{2} [\varepsilon(y) - \varepsilon(y - \pi r_c)]$$

2-nd derivative of $\sigma(y)$

$$\sigma''(y) = \kappa [\delta(y) - \delta(y - \pi r_c)]$$

Hierarchy relation

$$M_{\text{Pl}}^2 = \frac{M_5^3}{\kappa} \exp(2C)$$

Interaction Lagrangian (massive gravitons only)

$$L(x) = -\frac{1}{\Lambda_\pi} \sum_{n=1}^{\infty} h_{\mu\nu}^{(n)}(x) T_{\alpha\beta}(x) \eta^{\mu\alpha} \eta^{\nu\beta}$$

Masses of KK gravitons (x_n are zeros of $J_1(x)$)

$$m_n = x_n \frac{M_{\text{Pl}}}{\sqrt{\exp(2\pi\kappa r_c) - 1}} \left(\frac{\kappa}{M_5} \right)^{3/2}$$

Masses of KK gravitons m_n and coupling Λ_π
depend on C via M_5 and κ



Different values of C result in
quite diverse physical models

Two interesting physical scenarios

I. $\mathbf{C} = \mathbf{0}$

$$\sigma(0) = 0, \quad \sigma(\pi r_c) = \kappa \pi r_c$$



$$M_{\text{Pl}}^2 \cong \frac{M_5^3}{\kappa}$$

that requires

$$M_5 \sim \kappa \sim M_{\text{Pl}}$$

Masses of KK resonances

$$m_n \cong x_n \kappa \exp(-\kappa \pi r_c)$$



RS1 model (*Randall & Sundrum, 1999*)

Graviton spectrum - heavy resonances,
with the lightest one above 1 TeV

$$\text{II. } \mathbf{C} = \kappa \pi r_c$$

$$\sigma(0) = -\kappa \pi r_c, \quad \sigma(\pi r) = 0$$



$$M_{\text{Pl}}^2 \cong \frac{M_5^3}{\kappa} \exp(2\pi\kappa r_c)$$

$$\kappa \ll M_5$$

$$\kappa r_c \approx 9.5 \text{ for } M_5 = 1 \text{ TeV}, \kappa = 100 \text{ MeV}$$

Masses of KK resonances

$$m_n \cong x_n K$$



RSSC model: scenario with **small curvature**
of 5-dimensional space-time

For small **κ** , graviton spectrum is
similar to that of the ADD model

(*Giudice, 2005*
Petrov & A.K., 2005)

RSSC model vs. ADD model

RSSC model is **not** equivalent to the ADD model
with one flat ED of size $R=(\pi\kappa)^{-1}$ up to $\kappa \approx 10^{-18}$ eV

Hierarchy relation for small κ

$$M_{\text{Pl}}^2 \approx \frac{M_5^3}{\kappa} [\exp(2\pi\kappa r_c) - 1] \xrightarrow{2\pi\kappa r_c \ll 1} M_5^3 (2\pi r_c)$$

But the inequality $2\pi\kappa r_c \ll 1$ means that

$$\kappa \ll \frac{M_5^3}{M_{\text{Pl}}^2} \approx 0.17 \cdot 10^{-18} \left(\frac{M_5}{1 \text{TeV}} \right)^3 \text{eV}$$

Virtual Gravitons at the LHC

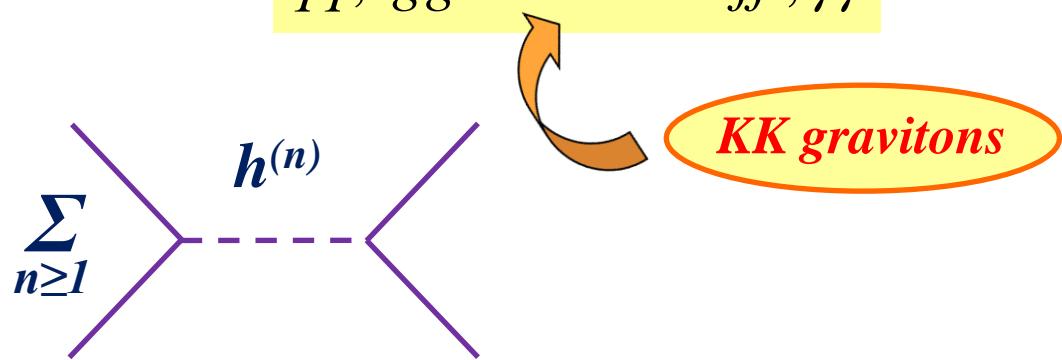
pp-collisions at LHC mediated by
KK graviton exchange in s-channel

Processes:

$$pp \rightarrow l^+l^- (\gamma\gamma, 2 \text{ jets}) + X$$

Sub-processes:

$$q\bar{q}, gg \rightarrow h^{(n)} \rightarrow f\bar{f}, \gamma\gamma$$



Matrix element of sub-process

$$M = A \times S$$

where

$$A = T_{\mu\nu}^{\text{in}} P^{\mu\nu\alpha\beta} T_{\alpha\beta}^f$$

*Tensor part of
graviton propagator*

Energy-momentum tensors

$$S(s) = \frac{1}{\Lambda_\pi^2} \sum_{n=1}^{\infty} \frac{1}{s - m_n^2 + i m_n \Gamma_n} \quad (\text{process independent})$$

Graviton widths

$$\Gamma_n = \eta m_n^3 / \Lambda_\pi^2, \quad \eta \cong 0.1$$

Recall that $m_n \cong z_n \kappa$

$$\sum_{n=1}^{\infty} \frac{1}{z_n^2 - z^2} = \frac{1}{2z} \frac{J_{\nu+1}(z)}{J_{\nu}(z)}, \quad J_{\nu}(z_n) = 0$$



$$S(s) \approx -\frac{1}{4\bar{M}_5^3 \sqrt{s}} \frac{\sin 2A + i \sinh 2\varepsilon}{\cos^2 A + \sinh^2 \varepsilon}$$

(A.K, 2006)

where

$$A = \frac{\sqrt{s}}{\kappa}, \quad \varepsilon = \frac{\eta}{2} \left(\frac{\sqrt{s}}{\bar{M}_5} \right)^3$$

Equivalent Photon Approximation (EPA)

Field of fast charged particle is similar
to electromagnetic radiation

(*Fermi, 1924; Weizsäcker, 1934; Williams, 1935*)

Spectrum of photon emitted by proton
(Q^2 is photon virtuality, $E_\gamma = \xi E$ its energy)

$$\frac{dN}{dE_\gamma dQ^2} = \frac{\alpha}{\pi} \frac{1}{E_\gamma Q^2} \left[\left(1 - \frac{E_\gamma}{E} \right) \left(1 - \frac{Q_{\min}^2}{Q^2} \right) F_E + \frac{E_\gamma^2}{2E^2} F_M \right]$$

(*Budnev et al., 1975*)

$$Q_{\min}^2 = \frac{m_p^2 E_\gamma^2}{E(E - E_\gamma)} \quad F_E = \frac{4m_p^2 G_E^2 + Q^2 G_M^2}{4m_p^2 + Q^2}$$

$$F_M = G_M^2$$

$$G_E^2 = \frac{G_M^2}{\mu_p^2} = \left(1 + \frac{Q^2}{Q_0^2} \right)^{-4} \quad Q_0^2 = 0.71 \text{ GeV}^2 \quad \mu_p^2 = 7.78$$

square of proton magnetic moment

Effective $\gamma\gamma$ -luminosity

$$\frac{dL_{\gamma\gamma}}{dW} = \int_{Q_{\min}^2}^{Q_{\max}^2} dQ_1^2 \int_{Q_{\min}^2}^{Q_{\max}^2} dQ_2^2 \int_{y_{\min}}^{y_{\max}} dy \frac{W}{2y} f_1\left(\frac{W^2}{4y}, Q_1^2\right) f_2(y, Q_2^2)$$

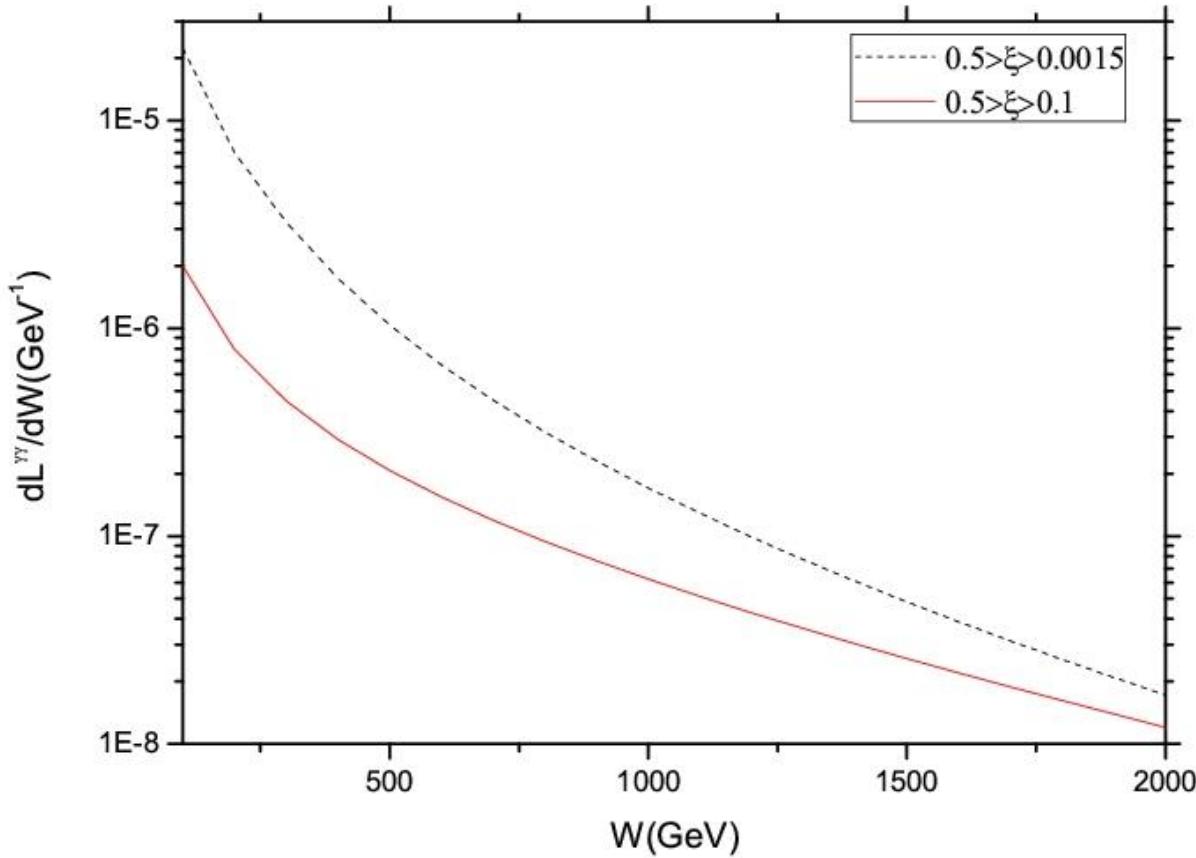
$$Q^2_{\max} = 2 \text{ GeV}^2$$

PDFs

Cross section for the process $\text{pp} \rightarrow \text{p}\gamma\gamma\text{p} \rightarrow \text{p}X\text{p}$

$$d\sigma = \int \frac{dL_{\gamma\gamma}}{dW} d\sigma_{\gamma\gamma \rightarrow X}(W) dW$$

W = invariant energy of two photons



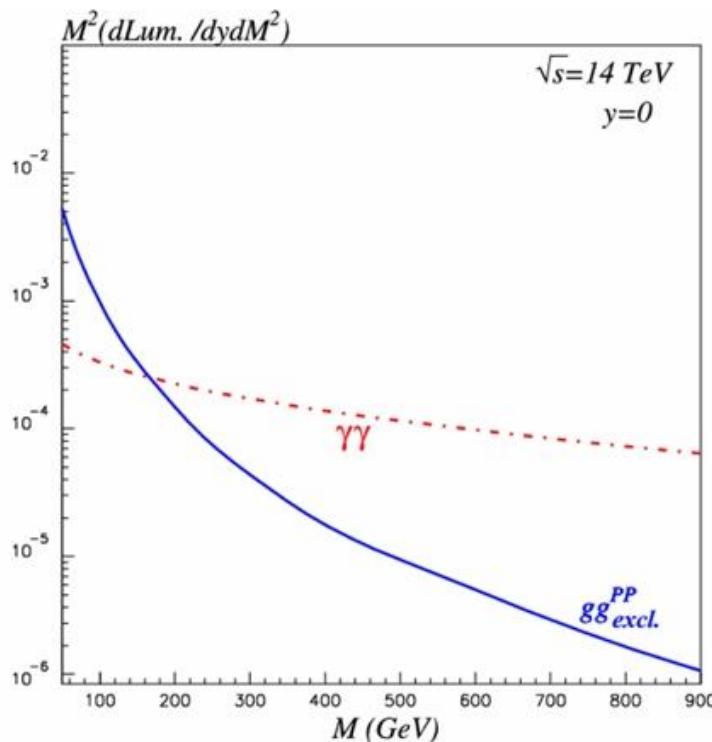
**Effective $\gamma\gamma$ luminosity (in GeV^{-1}) as a function
of invariant mass of two photons
(forward detector acceptance: $0.0015 (0.1) < \xi < 0.5$)**

$\gamma\gamma$ process vs. gluon induced process

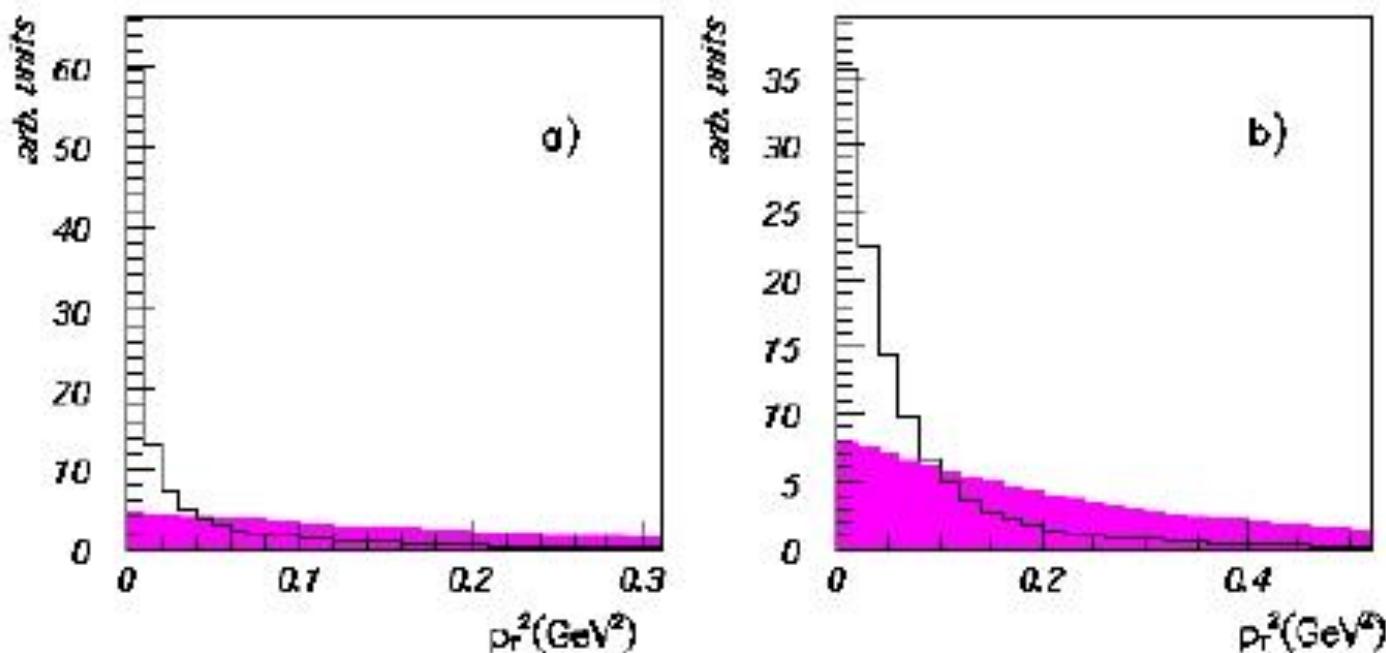
*Exclusive event requires no extra
gluon radiation into final state*



*Sudakov suppression in QCD cross section leads
to enhancement in $\gamma\gamma$ for $M_x > 150\text{-}200\text{ GeV}$*



$\gamma\gamma$ process vs. double-Pomeron exchange



*True (a) and observed (b) p_t^2 distribution of scattered protons in photo-production (line) and diffraction (filled histogram)
(in arbitrary units)*

$$p_t^2 < 0.005 \text{ GeV}^2$$



*Diffractive contribution
is significantly reduced*

Matrix element squared consists of electromagnetic, KK and interference terms

$$|M|^2 = |M_{\text{em}}|^2 + |M_{KK}|^2 + |M_{\text{int}}|^2$$

$$|M_{\text{em}}|^2 = -2e^4 \left[\frac{\hat{s} + \hat{t}}{\hat{t}} + \frac{\hat{t}}{\hat{s} + \hat{t}} \right]$$

$$|M_{KK}|^2 = \frac{1}{4} |S(\hat{s})|^2 \left[-\frac{\hat{t}}{8} (\hat{s}^3 + 2\hat{t}^3 + 3\hat{t}\hat{s}^2 + 4\hat{t}^2\hat{s}) \right]$$

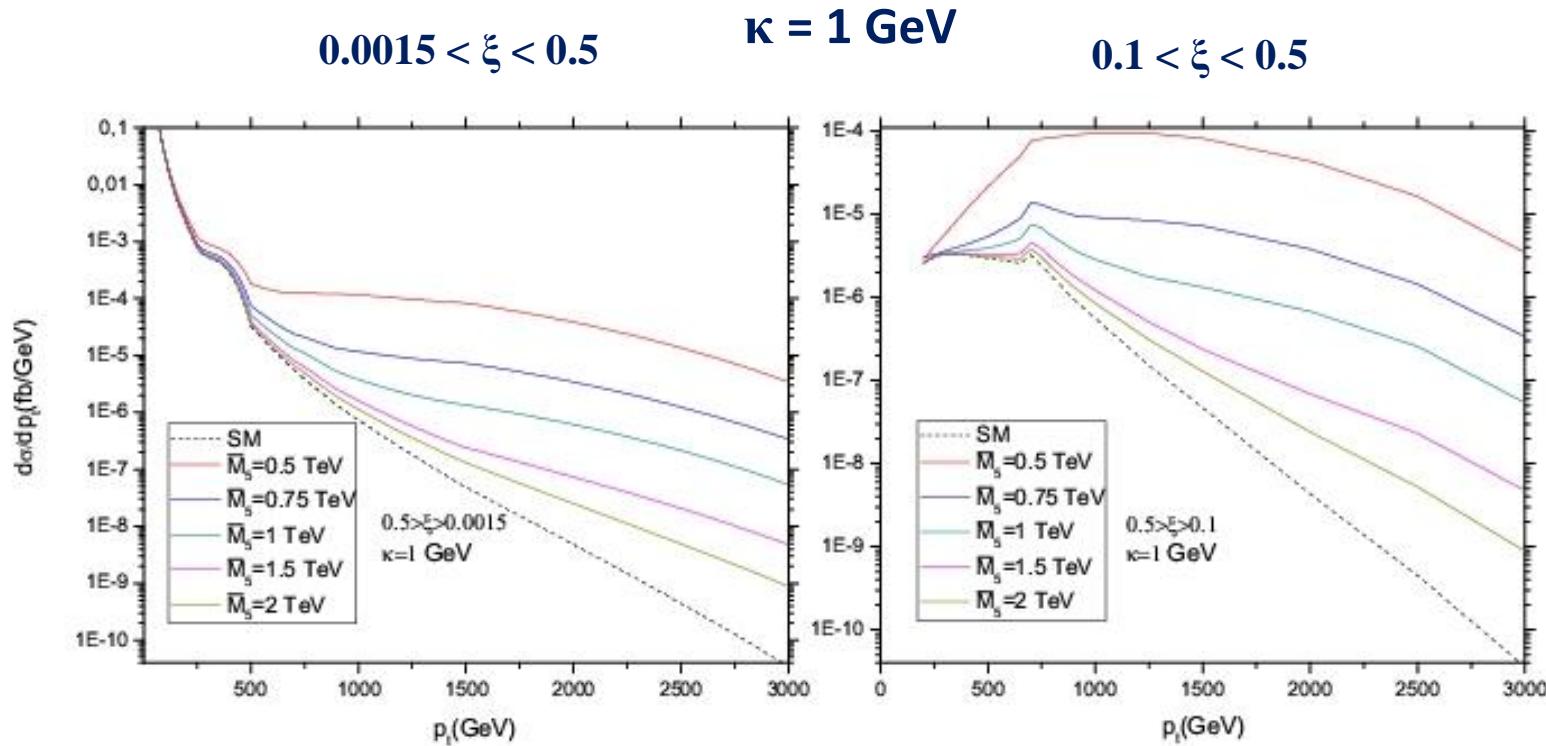
$$|M_{\text{int}}|^2 = -\frac{1}{4} e^2 \mathbf{Re} S(\hat{s}) (\hat{s}^2 + 2\hat{t}^2 + 2\hat{s}\hat{t})$$

\hat{s}, \hat{t} are Mandelstam variables
of sub-process $\gamma\gamma \rightarrow \mu^+\mu^-$

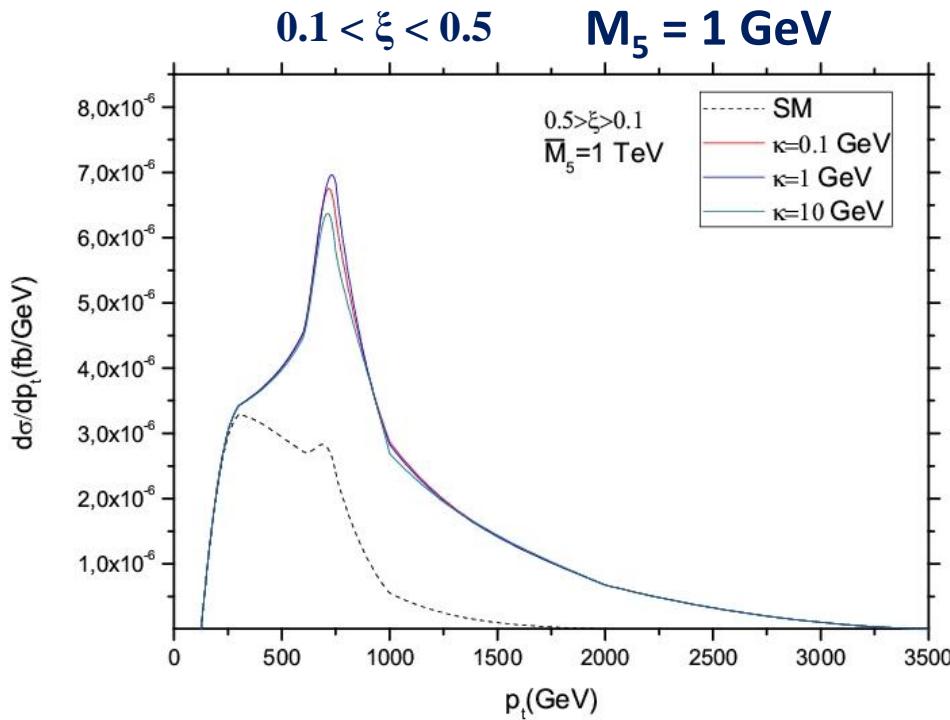
Differential and total cross sections

Cuts on transverse momenta of final muons and their rapidities:

$$p_t > 30 \text{ GeV}, |\eta| < 2.4$$



Differential cross section (in fb/GeV) for the process
 $pp \rightarrow p\gamma\gamma p \rightarrow p\mu^+\mu^-p$ as a function
of transverse momenta of final muons p_t



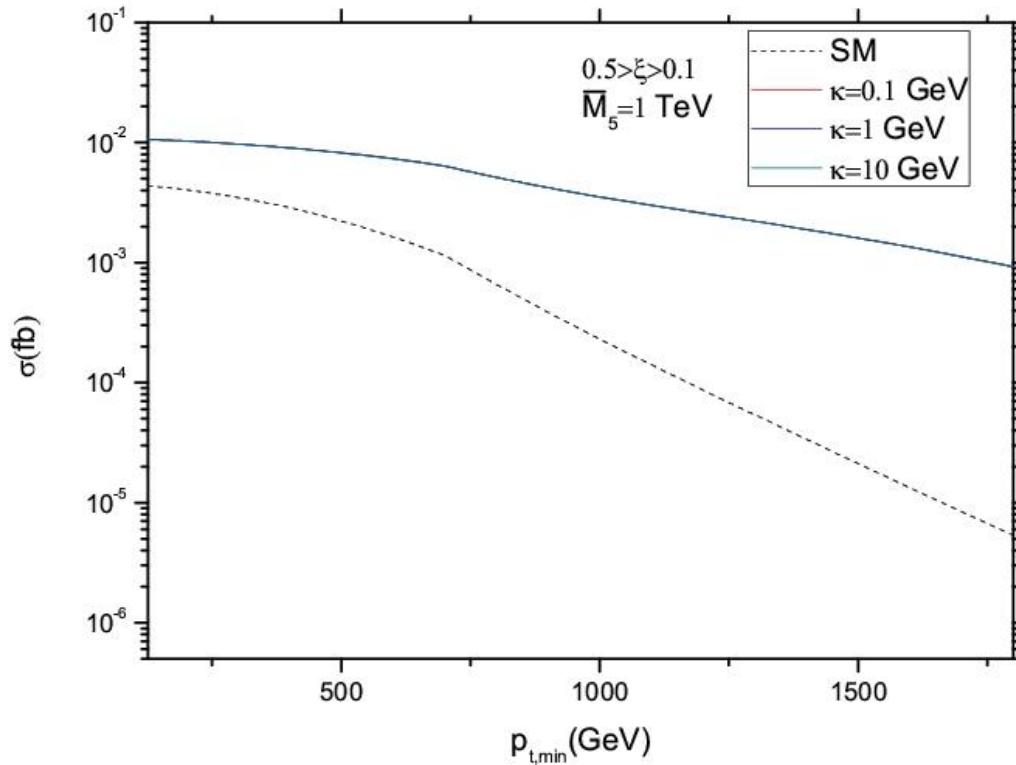
**Differential cross section for the process
 $\text{pp} \rightarrow p\gamma\gamma p \rightarrow p\mu^+\mu^-p$ for different values
of the curvature parameter κ**



**No noticeable dependence
on parameter κ**

Total cross section as a function of minimal transverse momentum of final muons $p_{t,\min}$

$$\sigma(p_t > p_{t,\min}) = \int_{p_{t,\min}} \frac{d\sigma}{dp_t} dp_t$$

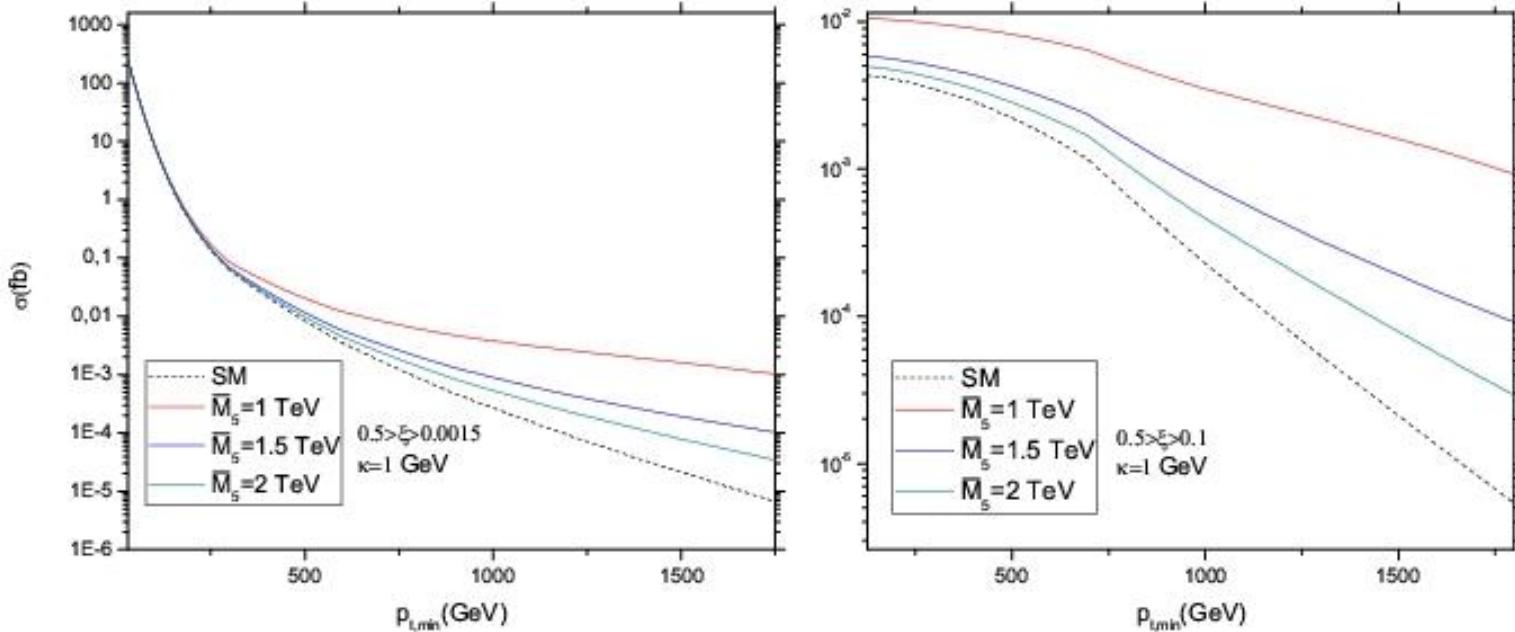


Total cross section (in fb) for the process
 $\text{pp} \rightarrow \rho \gamma \gamma \rho \rightarrow \rho \mu^+ \mu^- \rho$ **as a function of minimal**
transverse momentum of final muons $p_{t,\min}$ **for different values of κ**

$0.0015 < \xi < 0.5$

$\kappa = 1 \text{ GeV}$

$0.1 < \xi < 0.5$



Total cross section for the process
 $\text{pp} \rightarrow \text{p}\gamma\gamma\text{p} \rightarrow \text{p}\mu^+\mu^-\text{p}$ as a function of minimal
transverse momentum of final muons $p_{t,\min}$
for different values of M_5



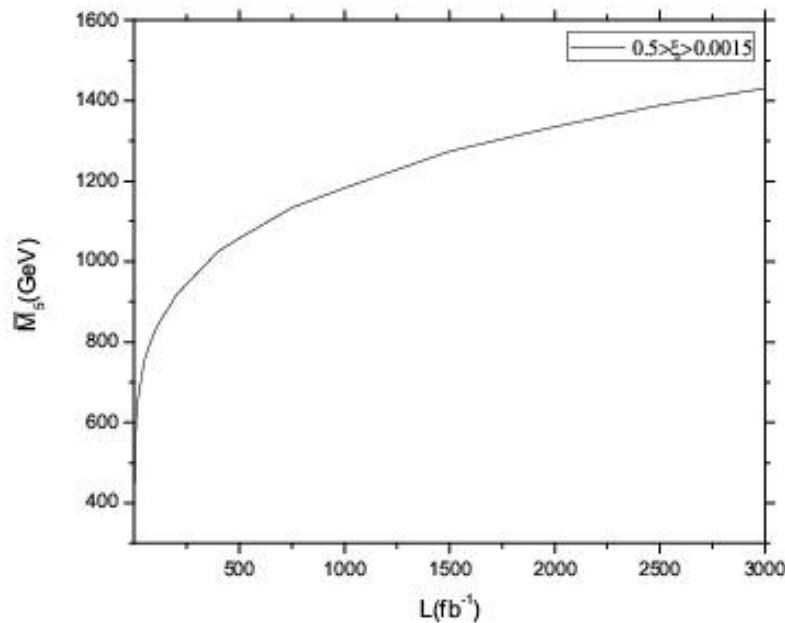
Statistical significance

$$S = \sqrt{2 \left[(N_S + N_B) \ln(1 + N_S / N_B) - N_S \right]}$$

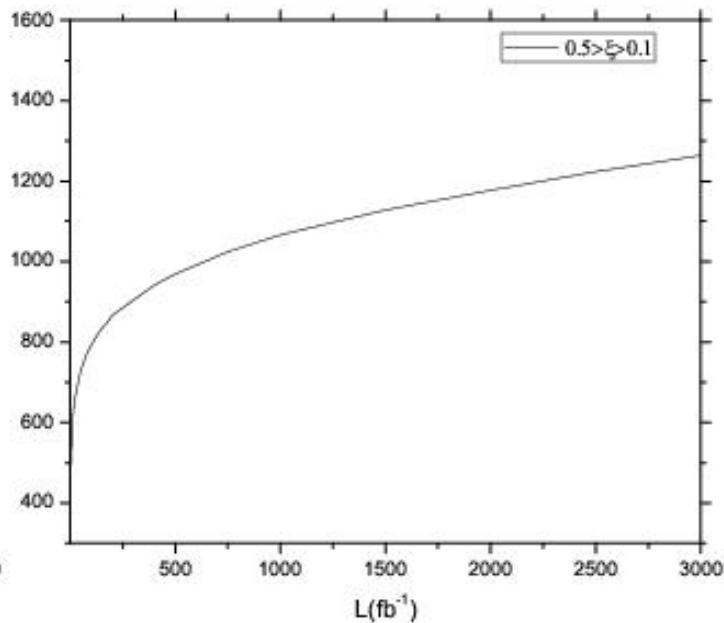
N_S (N_B) - number of signal
(background) events

$$S \approx \frac{N_S}{\sqrt{N_B}}, \quad N_S \ll N_B$$

$0.0015 < \xi < 0.5$
 $p_t > 500 \text{ GeV}$



$0.1 < \xi < 0.5$
 $p_t > 30 \text{ GeV}$



**95% C.L. search limit for 5-dimensional Planck scale
 M_5 as a function of integrated LHC luminosity
with cuts $p_t > 500 \text{ GeV}$ (30 GeV), $|\eta| < 2.4$ imposed**

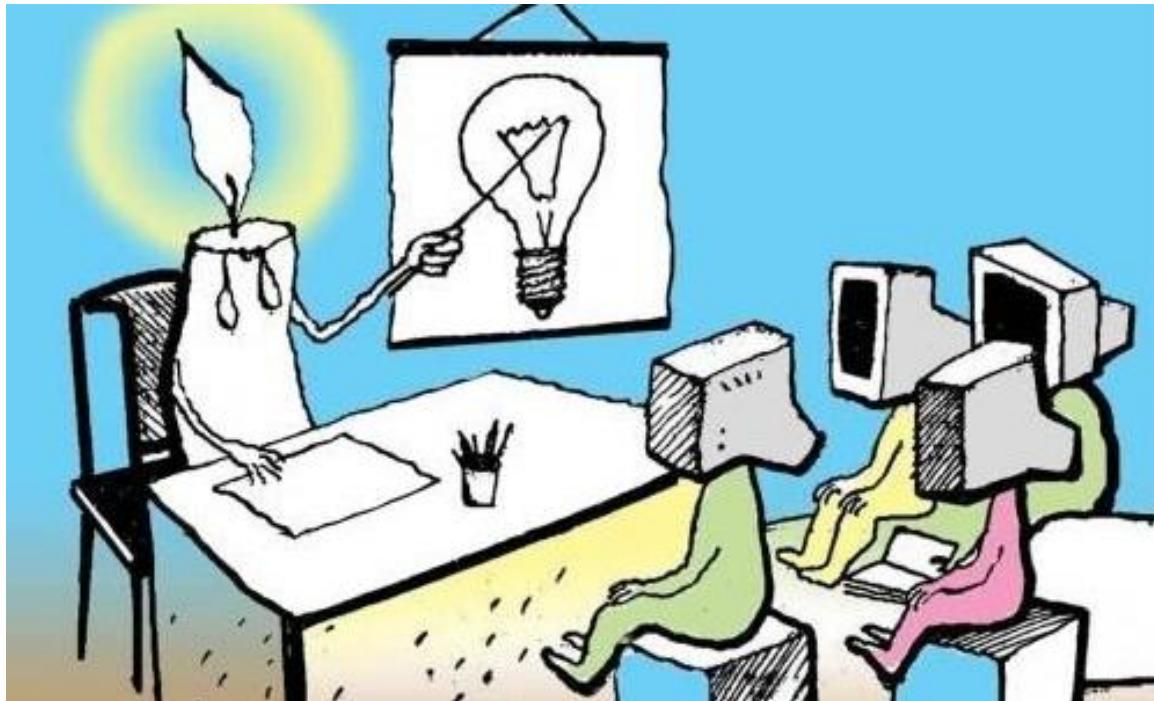
Заключение

- В рамках модели с одной дополнительной размерностью и малой кривизной пространства-времени изучено рождение пары мюонов на БАК в процессе, индуцированном фотонами.
- Обобщенное решение для метрики в рассмотренной модели:
 - симметрично относительно обеих бран;
 - имеет на них правильные скачки;
 - совместимо с симметриями орбифолда;
 - зависит от константы.

Заключение (продолжение)

- Начальные $\gamma\gamma$ -состояния естественно приводят к эксклюзивному рождению с «неповреждёнными» протонами на БАК.
- Нами вычислены дифференциальное и полное сечения процесса $p p \rightarrow p \gamma\gamma p \rightarrow p \mu^+ \mu^- p$ при энергии 14 ТэВ.
- С достоверностью 95% оценены значения 5-ти мерной массы Планка M_5 , доступные для обнаружения на БАК в данном процессе (например, $M_5 = 1 - 1.2$ ТэВ для $L = 1000$ фб⁻¹).
- Результат не зависит от другого параметра модели k , определяющего кривизну пространства-времени, при условии $k \ll M_5$.

Спасибо за внимание!



Back-up slides

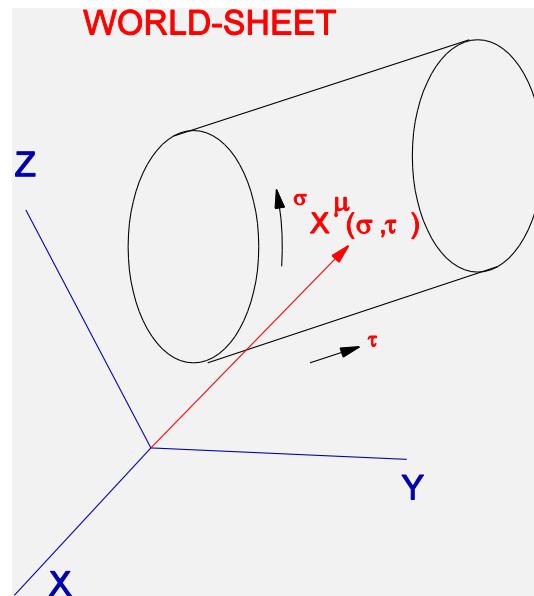
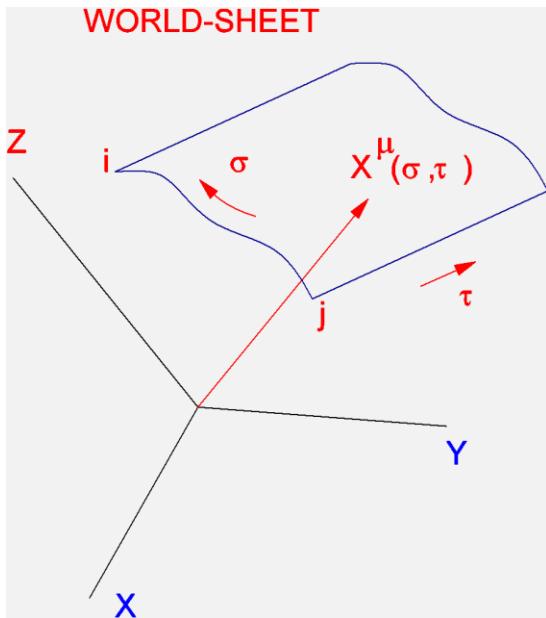
n	Obs. limit [TeV]	Exp. limit [TeV]
3	2.85	3.32
4	2.86	3.29
5	2.88	3.28
6	2.90	3.28

95% C.L. expected and observed lower limits on D-dimensional Planck scale M_D ($D=4+n$) as a function of number of extra dimensions n in the ADD model
 (CMS, 13 TeV, 35.9 fb^{-1})

(CMS Collaboration, arXiv:1810.00196)

Strings needs extra dimensions (EDs)

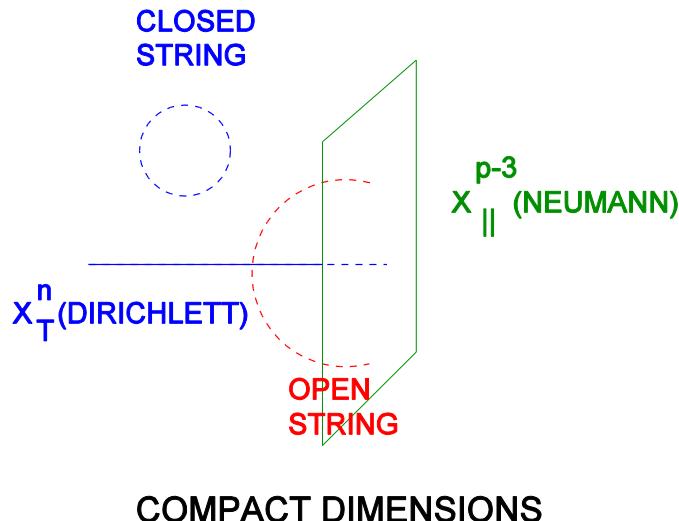
**Superstrings: D= 10
(6 EDs must be compactified)**



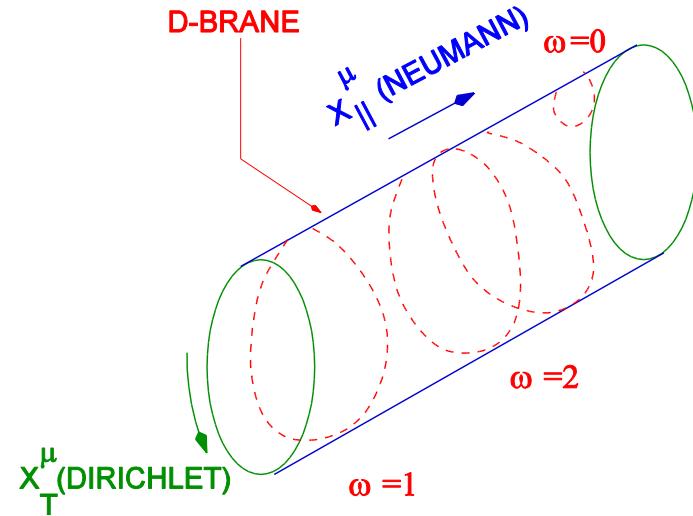
World sheets of open (left) and closed (right)
strings propagating in the space-time

Propagation of strings in extra dimensions

**Six internal compact dimensions:
(p-3) longitudinal , n = (9-p) transverse**



**Closed strings propagate
in the bulk**



**Open strings propagate
with ends at $x_T = \text{const}$
for different windings**

- string scale
- string coupling
- Planck scale
- gauge coupling

$$M_S = l_S^{-1}$$

$$\lambda_S$$

$$M_{\text{Pl}} = l_{\text{Pl}}^{-1}$$

$$g$$

string tension $\alpha' = M_S^{-2}$

6 internal compact dimensions:
 (p-3) longitudinal ,
 n = (9-p) transverse

Ten-dimensional action

$$S = \int_{\text{bulk}} d^{10}x \frac{1}{\lambda_S^2} l_S^{-8} R + \int_{\text{brane}} d^{p+1}x \frac{1}{\lambda_S} l_S^{3-p} F^2$$

Upon compactification of EDs:

$$\frac{1}{l_{\text{Pl}}^2} = \frac{V_L V_T}{\lambda_S^2 l_S^8}$$

$$\frac{1}{g^2} = \frac{V_L}{\lambda_S l_S^{p-3}}$$

**D-dimensional
Planck scale (D=4+n)**

$$M_D^{2+n} = M_S^{2+4} / (g^4 V_L l_s^{3-p})$$



Hierarchy relation

$$M_{\text{Pl}}^2 = M_D^{2+n} R_T^n$$

Explicit account of periodicity and Z_2 -symmetry

Solution for the warp function in variable

$x = y/r_c$ (A.K., 2015)

$$\sigma(y) = \frac{\kappa r_c}{2} \left[|\text{Arccos}(\cos x)| - |\text{Arccos}(\cos x) - \pi| \right] + \frac{\pi \kappa r_c}{2} - C$$

Arccos(z) is principal value of inverse cosine

$$0 \leq \text{Arccos}(z) \leq \pi, \quad -1 \leq z \leq 1$$

$$\text{Arccos}(\cos x) = \begin{cases} x - 2n\pi, & 2n\pi \leq x \leq (2n+1)\pi \\ -x + 2(n+1)\pi, & (2n+1)\pi \leq x \leq 2(n+1)\pi \end{cases}$$

(see, for instance, Gradshteyn & Ryzhik)

In particular, $\sigma(y) = \kappa y$ for $0 \leq y \leq \pi r_c$

➡ Orbifold symmetries:

$$\sigma(y + 2\pi r_c) = \sigma(y) \quad (\text{periodicity})$$

$$\sigma(-y) = \sigma(y) \quad (\mathbf{Z}_2 \text{ symmetry})$$

1-st derivative of $\sigma(y)$: ($y \neq \pi n r_c$, $n = 0, \pm 1, \pm 2, \dots$)

$$\sigma'(y) = \kappa \operatorname{sign}(\sin(x)) \quad \sigma'(-y) = -\sigma'(y)$$

2-nd derivative of $\sigma(y)$:

$$\sigma''(y) = \frac{\kappa}{r_c} \sum_{n=-\infty}^{\infty} [\delta(x + 2\pi n) - \delta(x - \pi + 2\pi n)]$$



Orbifold symmetries:

$$\sigma(y + 2\pi r_c) = \sigma(y) \quad (\text{periodicity})$$

$$\sigma(-y) = \sigma(y) \quad (\mathbb{Z}_2 \text{ symmetry})$$

1-st derivative of $\sigma(y)$: ($y \neq \pi n r_c$, $n = 0, \pm 1, \pm 2, \dots$)

$$\sigma'(y) = \kappa \operatorname{sign}[\sin(y/r_c)]$$

$$\sigma'(-y) = -\sigma'(y)$$

2-nd derivative of $\sigma(y)$:

$$\sigma''(y) = \kappa \sum_{n=-\infty}^{\infty} [\delta(y + 2\pi n r_c) - \delta(y - \pi r_c + 2\pi n r_c)]$$

$$\sigma''(-y) = \sigma''(y)$$

III. $C = \kappa\pi r_c/2$

$$\sigma(0) = -\sigma(\pi r_c) = \kappa\pi r_c/2$$

“symmetric”
scheme



$$M_{\text{Pl}}^2 \cong \frac{2M_5^3}{\kappa} \sinh(2\pi\kappa r_c)$$

Masses of gravitons

$$m_n \cong x_n \kappa \exp(-\kappa\pi r_c/2)$$

Let

$$M_5 = 2 \cdot 10^9 \text{ GeV}, \kappa = 10^4 \text{ GeV}$$

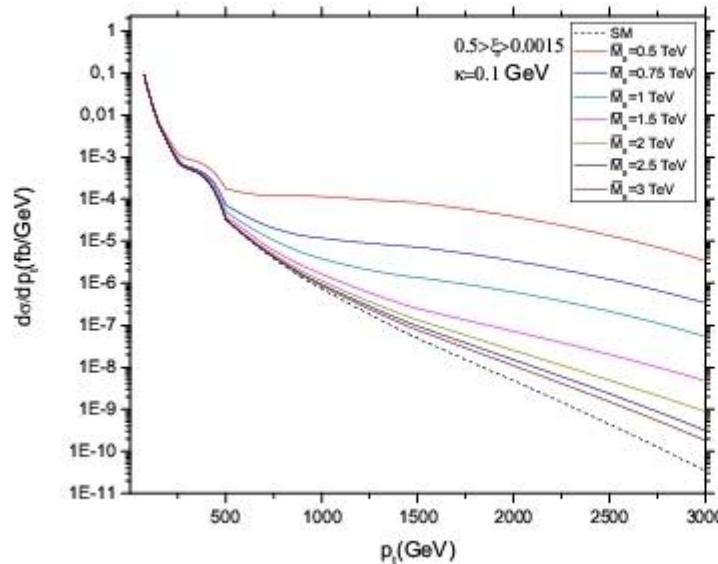


$$m_n \cong 3.7 x_n (\text{MeV}) \quad (\text{A.K., 2015})$$

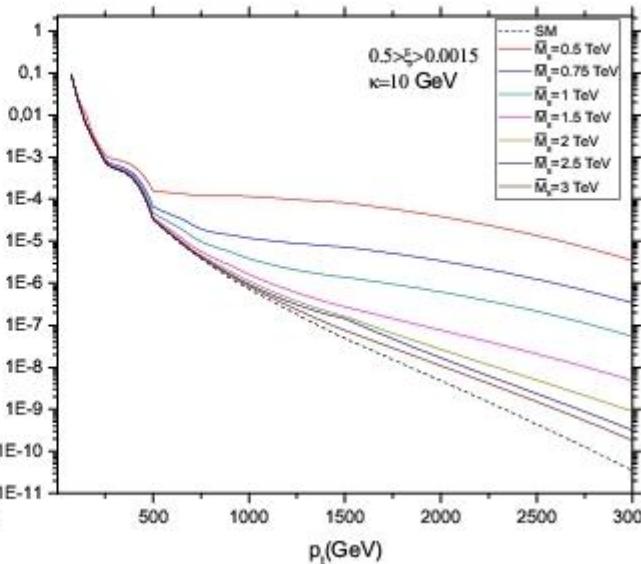
**Almost continuous spectrum
of KK gravitons**

$$0.0015 < \xi < 0.5$$

$\kappa = 0.1 \text{ GeV}$



$\kappa = 1 \text{ GeV}$



**Dependence of differential cross section
for the process $pp \rightarrow p\gamma\gamma p \rightarrow p\mu^+\mu^-p$
on curvature parameter κ**